

Corrigendum to the paper:

On the strong summability of orthogonal series*)

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Professor G. SUNOUCHI kindly drew my attention to a gap in Lemma 3. The given proof of this lemma is correct only in that case if under the condition (3. 1) $\frac{pk}{p-1} = 2$ is fulfilled instead of $\frac{pk}{p-1} \cong 2$.¹⁾ Consequently, the conditions of the theorems are satisfied only for $k < 2$, so the theorems and corollaries are also valid for such powers k .

However, instead of Lemma 3, we can prove the following

Lemma. Let $k > 0$ and $\sum c_n^2 < \infty$. If there exists a $p > 1$ such that the conditions (3. 1) are satisfied, then for $\gamma > 1 - \frac{p-1}{pk}$ we have

$$\int_a^b \left\{ \sup_{1 \leq n < \infty} \left(\frac{1}{A_n} \sum_{v=0}^n \alpha_{nv} |\sigma_v^{\gamma-1}(x) - \sigma_v^\gamma(x)|^k \right)^{1/k} \right\}^2 dx \cong K \sum_{n=0}^{\infty} c_n^2.$$

Using this lemma we obtain that Theorem 1 and 2, for arbitrary $k > 0$ but with $\gamma > 1 - \frac{p-1}{pk}$ instead of $\gamma > \frac{1}{2}$, remain valid.

The modified theorems also include the theorems of SUNOUCHI²⁾.

Proof of Lemma. We have as in the proof of Lemma 3 that

$$\begin{aligned} & \int_a^b \left\{ \sup_{1 \leq n < \infty} \left(\frac{1}{A_n} \sum_{v=0}^n \alpha_{nv} |\sigma_v^{\gamma-1}(x) - \sigma_v^\gamma(x)|^k \right)^{1/k} \right\}^2 dx \cong \\ & \cong K_1 \int_a^b \left(\sum_{v=1}^{\infty} v^{-1} |\sigma_v^{\gamma-1}(x) - \sigma_v^\gamma(x)|^{qk} \right)^{2/qk} dx. \end{aligned}$$

*) *Acta Sci. Math.*, 27 (1966), 217–228.

¹⁾ We use the same notation as in the paper.

²⁾ G. SUNOUCHI, On the strong summability of orthogonal series, *Acta. Sci. Math.*, 27 (1966), 71–79.

Using a theorem of FLETT³⁾ we obtain that

$$\int_a^b \left(\sum_{v=1}^{\infty} v^{-1} |\sigma_v^{\gamma-1}(x) - \sigma_v^{\gamma}(x)|^{qk} \right)^{2/qk} dx \cong K_2 \int_a^b \left(\sum_{v=1}^{\infty} v^{-1} |\sigma_v^{\alpha-1}(x) - \sigma_v^{\alpha}(x)|^2 \right) dx,$$

where $\frac{1}{2} < \alpha < \gamma - \frac{1}{2} + \frac{p-1}{pk}$.

From this, by Lemma 2, we get the statement of the Lemma.

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³⁾ On an extension of absolute summability and some theorems of LITTLEWOOD and PALEY, *Proc. London Math. Soc.*, 7 (1957), 113—141, cf. in particular p. 115.